

M R

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مدرس خصوصي

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اونلاين

يُحصل الطالب علي

• مقاطع فيديو هات لشرح المقرر بشكل وافي

• ملخص للمادة Pdf للمذاكرة والمراجعة

• محاضرات مباشرة علي برنامج زووم

• مناقشة الأجزاء الغير مفهومة

• تواصل مستمر مع معلم المادة

للتواصل

0567630097

0565657741



Example No (5)

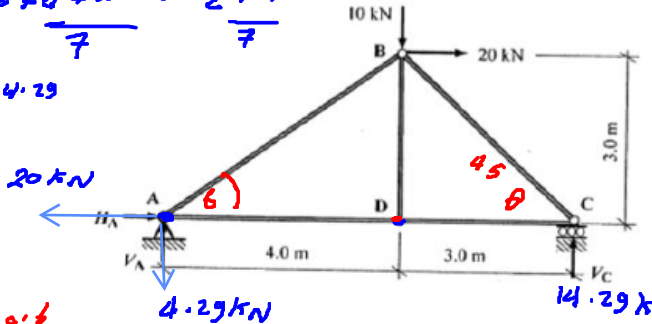
Consider the truss indicated below determine the vertical deflection at joint D assuming the existing loading and member BC is too short by 2mm, member CD is too longer by 1.5mm and that members AD and CD are both subject to an increase in temperature of 5°C.

Assume $\alpha = 12.0 \times 10^{-6}/^{\circ}\text{C}$ and $AE = 100 \times 10^3 \text{ kN}$.

Determine the vertical deflection at joint D due to combined loading, lack-of-fit and temperature change using Virtual Work Principles

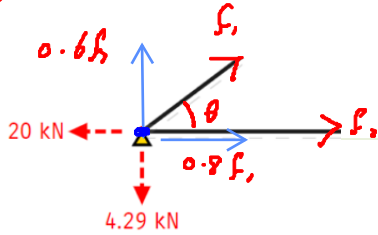
$$\sum F_y = 10 \times 1 + 20 \times 1 = V_c \times 7$$

$$V_c = 14.29$$



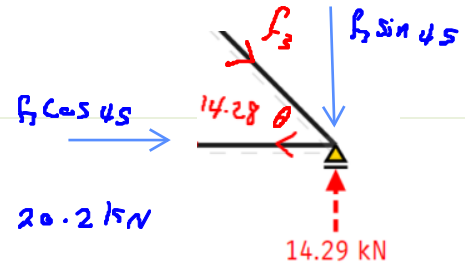
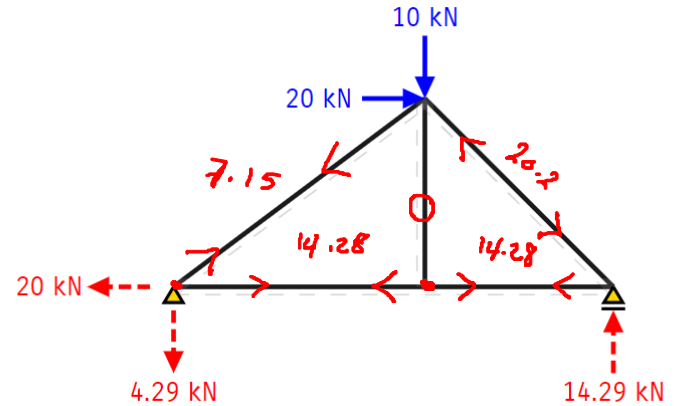
$$\sin 6 = 0.6$$

$$\cos 6 = 0.8$$



$$f_1 = \frac{4.29}{0.6} = 7.15 \text{ kN}$$

$$f_2 = 20 - 0.8 \times 7.15 = 14.28 \text{ kN}$$



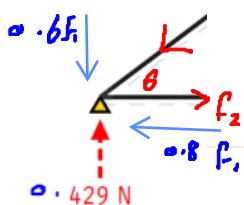
$$f_3 = \frac{14.29}{\sin 45} = 20.2 \text{ kN}$$

$$\sum F_y = 1 + 4 = V_c \times 7$$

$$V_c = \frac{5}{7} = 0.714 \text{ kN}$$

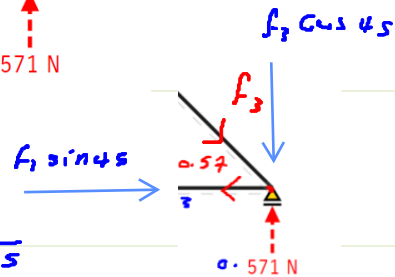
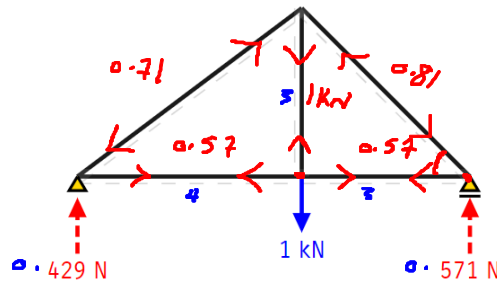
$$\sin 6 = 0.6$$

$$\cos 6 = 0.8$$



$$f_1 = \frac{0.429}{0.6} = 0.71 \text{ kN}$$

$$f_2 = 0.8 \times 0.71 = 0.57 \text{ kN}$$



$$f_3 = \frac{0.57}{\sin 45}$$

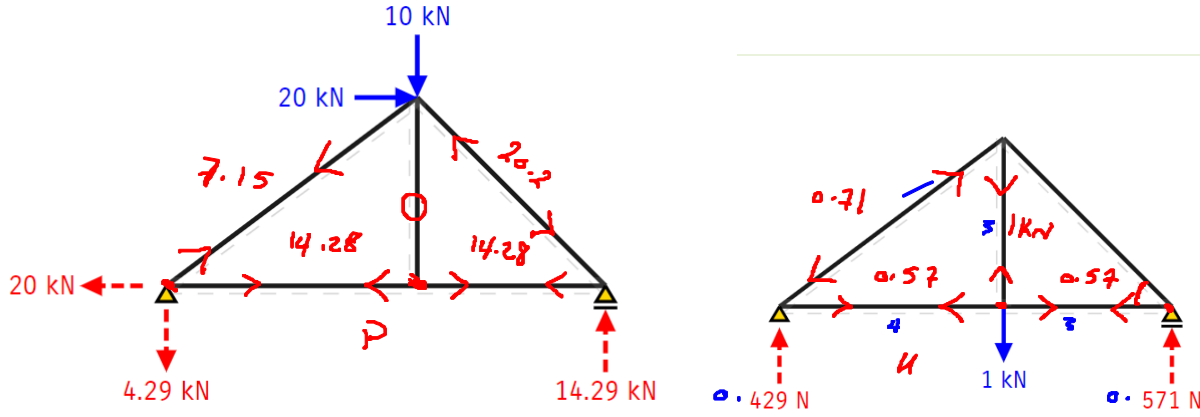
$$= 0.81 \text{ kN}$$

Consider the truss indicated below determine the vertical deflection at joint D assuming the existing loading and member BC is too short by 2mm, member CD is too longer by 1.5mm and that members AD and CD are both subject to an increase in temperature of 5°C .

Assume $\alpha = 12.0 \times 10^{-6}/^{\circ}\text{C}$ and $AE = 100 \times 10^3 \text{ kN}$.

Determine the vertical deflection at joint D due to combined loading, lack-of-fit and temperature change using Virtual Work Principles

$$\begin{aligned} \Delta_T &= \alpha \Delta T = 12 \times 10^{-6} \times 4 \times 5 \\ &= 0.24 \text{ mm} \\ \Delta_T &= 12 \times 10^{-6} \times 3 \times 5 \\ &= -0.18 \text{ mm} \end{aligned}$$



Member	Length (mm)	AE (kN)	(P-force (kN))	$\frac{PL}{AE}$ (mm)	Δ_L (mm)	Δ_T (mm)	u	$(\frac{PL}{AE} + \Delta_L + \Delta_T) \times u$ (mm)
AB	5000	100×10^3	+ 7.15	+ 0.36	0	0	- 0.71	- 0.26
BC	4243	100×10^3	- 20.20	- 0.86	- 2.0	0	- 0.81	+ 2.32
AD	4000	100×10^3	+ 14.29	+ 0.57	0	+ 0.24	+ 0.57	+ 0.46
CD	3000	100×10^3	+ 14.29	+ 0.43	+ 1.5	+ 0.18	+ 0.57	+ 1.20
BD	3000	100×10^3	0	0	0	0	1.0	0
								$\Sigma = + 3.72$

The vertical deflection at joint D due to combined loading, lack-of-fit and temperature change is given by:

$$\delta_{v,D} = \sum \left(\frac{PL}{AE} + \Delta_L + \Delta_T \right) \times u = + 3.72 \text{ mm} \downarrow$$