

M R

Ahmed Mahdy



مدرس خصوصي

حضورى

اونلاين

يحصل الطالب علي

مقاطع فيديو هات لشرح المقرر بشكل وافي

ملخص للمادة Pdf للمذكرة واطراجة

محاضرات مباشرة علي برنامج زووم

مناقشة الأجزاء الغير مفهومة

تواصل مستمر مع معلم المادة

للتواصل

0567630097

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Solved Examples

(Momentum Equation)

Example 1

A 600mm diameter pipeline carries water under a head of 30m with a velocity of 3m/s. This water main is fitted with a horizontal bend which turns the axis of the pipeline through 75° (i.e. the internal angle at the bend is 105°). Calculate the resultant force on the bend and its angle to the horizontal.

$$\sum F = f_T = \rho Q (v_2 - v_1)$$

$$A = \pi r^2 = \pi \left(\frac{d}{2} \right)^2 = \pi \frac{d^2}{4}$$

$$Q = A \cdot v$$

$$= \pi \times \frac{0.6^2}{4} \times 3$$

$$Q = 0.848 \text{ m}^3/\text{s}$$

$$f_T = \rho Q (v_2 - v_1)$$

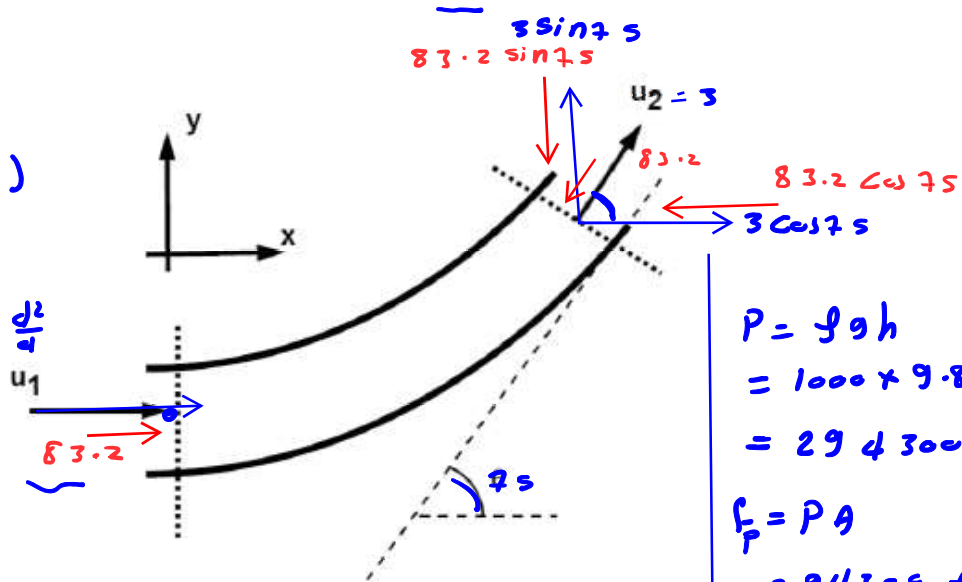
$$f_{Tx} = 1000 \times 0.848 (3 \cos 75^\circ - 3) = -1.886 \text{ kN}$$

$$\sum F_y = f_T = \rho Q (v_2 - v_1) = 1000 \times 0.848 (3 \sin 75^\circ)$$

$$f_{Ty} = 2.457 \text{ kN}$$

$$f_{Tx} = f_{Rx} + f_{Px} + f_{Bx}$$

$$-1.886 = f_{Rx} + 83.2 - 83.2 \cos 75^\circ \Rightarrow f_{Rx} = 63.6 \text{ kN}$$



$$P = \rho g h$$

$$= 1000 \times 9.81 \times 3$$

$$= 294300 \text{ Pa}$$

$$f_P = P A$$

$$= 294300 \times \pi \frac{0.6^2}{4}$$

$$= 83.2 \text{ kN}$$

$$\Sigma f_y = 2.457 = f_{Ry} + R_{Py}$$

$$2.457 = f_{Ry} + (-82.2 \sin 75)$$

$$f_{Ry} = 82.82 \text{ kN}$$

the force in the fluid

$$f_{Rx} = 63.6, \quad f_{Ry} = -82.82$$

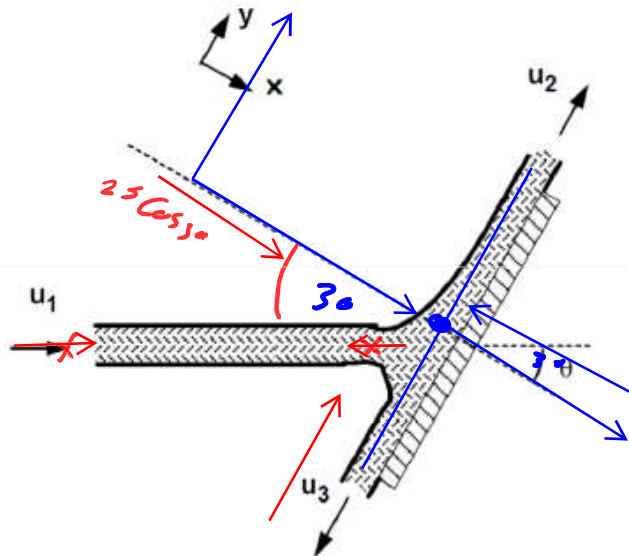
$$f_R = \sqrt{63.6^2 + 82.82^2} = 104.42 \text{ kN} \quad \theta = \tan^{-1}\left(\frac{-82.82}{63.6}\right) = -52.5^\circ$$

Example 2

A 75mm diameter jet of water having a velocity of 25m/s strikes a flat plate, the normal of which is inclined at 30° to the jet. Find the force normal to the surface of the plate.

$$A = \pi \frac{d^2}{4} = \pi \times \frac{(0.075)^2}{4} = 4.42 \times 10^{-3} \text{ m}^2$$

$$Q = A \cdot V = 0.11 \text{ m}^3/\text{s}$$



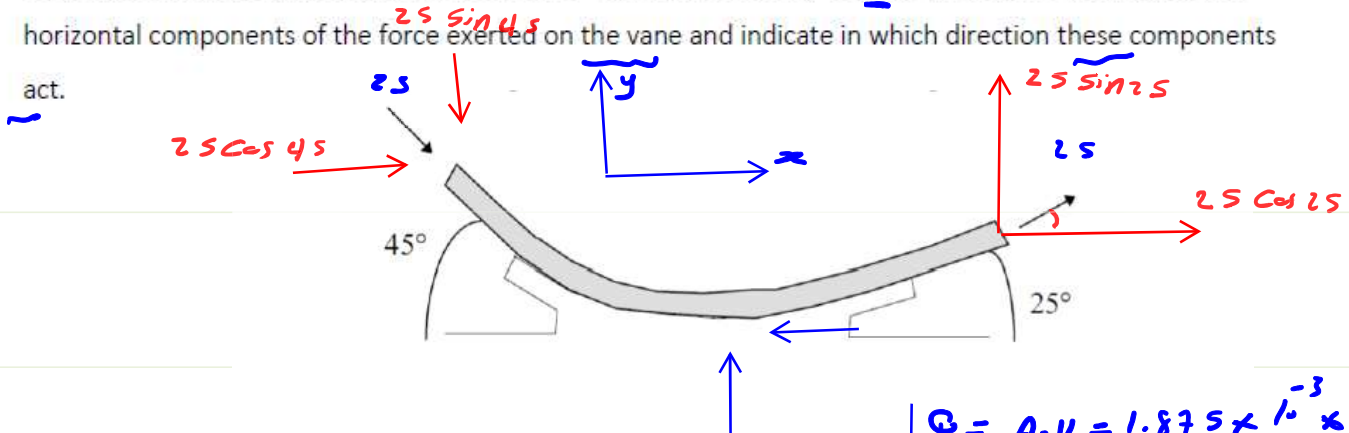
$$f_T = \rho Q (u_2 - u_1) = 1000 \times 0.11 (0 - 25 \cos 30)$$

$$f_T = -2.38 \text{ kN}$$

$$\underline{f_x} + \cancel{f_y} + \cancel{f_z} = \underline{-2.38 \text{ kN}}$$

Example 4.3

The figure below shows a smooth curved vane attached to a rigid foundation. The jet of water, rectangular in section, 75mm wide and 25mm thick, strike the vane with a velocity of 25m/s. Calculate the vertical and horizontal components of the force exerted on the vane and indicate in which direction these components



$$A = 75 \times 10^{-3} \times 25 \times 10^{-3} = 1.875 \times 10^{-3} \text{ m}^2$$

$$Q = A \cdot V = 1.875 \times 10^{-3} \times 25$$
$$Q = 46.875 \times 10^{-3} \text{ m}^3/\text{s}$$

$$F_x = \rho Q (v_{2x} - v_{1x})$$

$$1000 \times 46.875 \times 10^{-3} (25 \cos 25 - 25 \cos 45)$$

$$F_x = 233.44 \text{ N}$$

$$F_y = \rho Q (v_{2y} - v_{1y})$$

$$1000 \times 46.875 \times 10^{-3} (-25 \sin 25 + 25 \sin 45)$$

$$F_y = -333.38 \text{ N}$$

$$R_x = -233.44 \text{ N} \quad R_y = 333.38 \text{ N}$$